

# Semi-Supervised Learning and Feature Evaluation for RGB-D Object Recognition

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## Abstract

With new depth sensing technology such as Kinect providing high quality synchronized RGB and depth images (RGB-D data), combining the two distinct views for object recognition has attracted great interest in computer vision and robotics community. Recent methods mostly employ supervised learning methods for this new RGB-D modality based on the two feature sets. However, supervised learning methods always depend on large amount of manually labeled data for training models. To address the problem, this paper proposes a semi-supervised learning method to reduce the dependence on large annotated training sets. The method can effectively learn from relatively plentiful unlabeled data, if powerful feature representations for both the RGB and depth view can be extracted. Thus, a novel and effective feature termed CNN-SPM-RNN is proposed in this paper, and four representative features (KDES [1], CKM [2], HMP [3] and CNN-RNN [4]) are evaluated and compared with ours under the unified semi-supervised learning framework. Finally, We verify our method on three popular and publicly available RGB-D object databases. The experimental results demonstrate that, with only 20% labeled training set, the proposed method can achieve competitive performance compared with the state of the arts on most of the databases.

*Keywords:* RGB-D, object recognition, feature representation, feature evaluation, semi-supervised learning.

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## 1. Introduction

Recently, RGB-D data has attracted great interest in computer vision and robotics community with the advent of new depth sensors, such as Kinect. The Kinect-style depth cameras are capable of providing high quality synchronized images or videos of both color and depth, which represent an opportunity to dramatically improve the performance of many vision problems, e.g., object recognition [5, 6], detection [7, 8, 9], tracking [10, 11, 12], SLAM [13, 14] and human activity analysis [15, 16]. This is mainly because that depth information has many extra advantages: being invariant to lighting and color variations, allowing better separation from the background and providing pure geometry and shape cues. Furthermore, many RGB-D datasets [5, 6, 13, 14, 15, 17, 18] have been published for public use to promote the development of such research areas.

This paper mainly focuses on object recognition, which is a fundamental problem in computer vision and pattern recognition. Although many methods [1, 2, 3, 4, 19] have been presented to promote RGB-D object recognition, they chiefly aim at extracting effective features from the novel RGB-D data and using a supervised learning model to achieve good classification performance. However, supervised learning models always require for large amount of manually labeled data. The collection of enough labeled training set is an expensive and difficult task. Thus, it is important to get rid of this problem by utilizing relatively plentiful and convenient unlabeled RGB-D data.

With the ability to handle the unlabeled data, a semi-supervised learning framework is proposed in this paper by considering the two distinct views of RGB-D data effectively. Although there are many successful semi-supervised learning algorithms in the literature, e.g., self-training [20, 21, 22], co-training [23, 24] and graph-based methods [25, 26, 27], we are especially interested in the co-training method because of its unique advantages over the RGB-D data: co-training was theoretically proved to be very successful in combining the labeled and unlabeled data under two strong assumptions (including “conditional independence given the label”) in [23], then the work [24] proved that much weaker assumptions were sufficient to guarantee co-training, when given appropriately strong PAC-learning algorithms on each view. Intuitively, the two weaker assumptions can be described as follows: (1) Each example contains two distinct views, and each view provides sufficient information to determine the label of the example; (2) The two views should not be too highly correlated. It means that, there

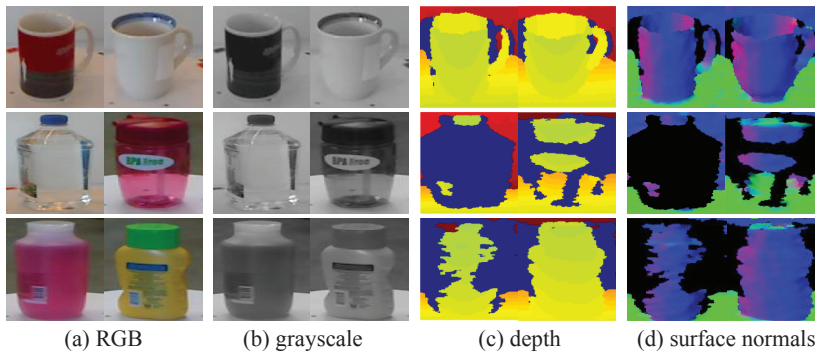


Figure 1: Four modalities including RGB, grayscale, depth, and surface normals are alternative to capture cues for RGB-D object recognition. RGB images and depth maps are directly imaged by Kinect-style cameras, while grayscale images and surface normals are computed from the RGB images and depth maps respectively. In the figure, each row consists of two instances from the same category (Examples are from the Washington RGB-D object dataset [6]).

34 should exist some examples which can be confidently recognized by one view but not  
 35 by the other view (or vice versa) to make the co-training algorithm work effectively.  
 36 RGB-D data meets the two assumptions very well. Firstly, RGB-D data contains two  
 37 distinct views, RGB and depth. Both of them can provide useful cues for object recog-  
 38 nition: RGB images can describe rich color, texture and appearance information for  
 39 the object, while depth maps can sketch pure geometry and shape cues. Secondly, the  
 40 image capturing modes of RGB (e.g., RGB cameras) and depth (e.g., infrared cameras)  
 41 are very different, guaranteeing the independence of the two views.

42 Given two distinct views (RGB and depth) for each example, the key to the suc-  
 43 cess of co-training is to obtain effective feature representation for each view. Thus a  
 44 powerful feature CNN-SPM-RNN will be proposed in this paper based on the feature  
 45 CNN-RNN [4]. CNN-RNN combines a single convolutional neural network (CNN)  
 46 and multiple recursive neural networks (RNN [28]) to learn high-level features for each  
 47 RGB-D object. Since learning the optimal structure of each RNN tree from the raw da-  
 48 ta is highly time consuming as described in [28], CNN-RNN utilizes fixed-tree RNN  
 49 structure to hierarchically aggregate the CNN responses very efficiently. However, the  
 50 fixed-tree RNN requires for the fixed-size of the inputs by simply cropping or warp-  
 51 ing all the images, which may degrade the recognition performance after such artificial  
 52 processing. **Inspired by the pioneer work [29], which applied a spatial pyramid pooling**  
 53 **layer (SPM [30]) to the supervised deep learning model [31] to adapt the model for ar-**  
 54 **bitrary sizes of inputs, we extend its core idea to the unsupervised CNN-RNN feature**

55 learning model and design a new feature learning structure, termed CNN-SPM-RNN.  
56 Towards SPM layer, the main differences between CNN-SPM-RNN and the work [29]  
57 are twofold: (1) A pooling layer with different pyramid partitions in [29] is sufficient  
58 to guarantee the success of the **supervised** deep learning model, benefiting from the  
59 back-propagation of errors and the fine-tuning of filters. However, we empirically  
60 find that a single pooling layer can even make the **unsupervised** CNN-RNN model  
61 worse, probably because the low-level convolutional responses cannot capture local  
62 object structures very effectively after pooling. Thus a feature coding layer is added  
63 to encode the convolutional responses and high-level feature responses are obtained to  
64 represent local information powerfully. Then the pooling layer is performed to result in  
65 fixed-scale feature maps for the fixed-tree RNNs. (2) Compared to the 2D spatial pyra-  
66 mid pooling for the RGB modality in [29], 3D spatial pyramid pooling is utilized for  
67 the depth modality to effectively capture shape cues of objects. The details are given  
68 in Section 2.2. Further more, we find that two additional modalities, grayscale images  
69 and surface normals, can largely benefit view representation, as shown in Fig. 1. We  
70 introduce a unified feature evaluation framework by combining RGB and grayscale to  
71 capture visual appearance (i.e., the RGB view), while depth and surface normals to  
72 capture shape cues (i.e., the depth view) for all the representative features, including  
73 KDES [1], CKM [2], HMP [3], CNN-RNN [4] and CNN-SPM-RNN.

74 An early version of our work was presented in [32] to explore co-training for RGB-  
75 D object recognition. In this paper, we extend [32] in the following aspects: developing  
76 a more powerful feature termed CNN-SPM-RNN based on [4, 32], introducing a uni-  
77 fied framework to fairly evaluate all the representative features, and presenting a wide  
78 array of experiments to demonstrate the effectiveness of the proposed semi-supervised  
79 method with powerful RGB-D features.

80 The major contributions of this paper are summarized as follows.

- 81 • Propose a complete and systematic semi-supervised learning framework for RGB-  
82 D object recognition using co-training. We theoretically analyse that the frame-  
83 work can take full advantage of the characteristics of the new RGB-D data, and  
84 significantly benefit object recognition by learning from large amount of unla-  
85 beled RGB-D data.
- 86 • Present a novel feature CNN-SPM-RNN to effectively represent RGB-D data.  
87 To the best of our knowledge, this is the first work to successfully apply SPM

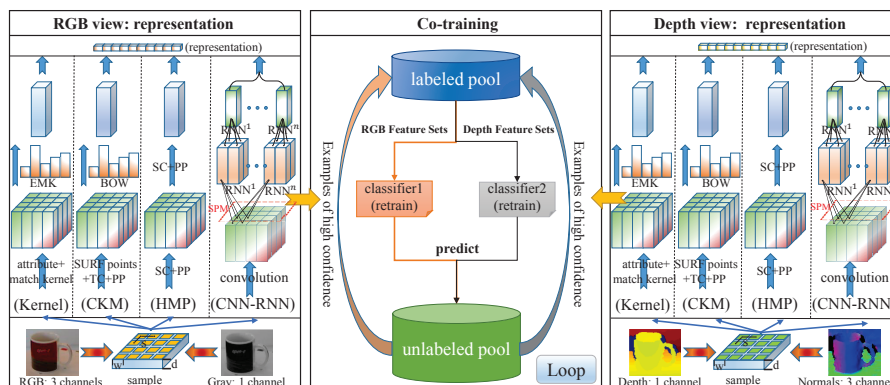


Figure 2: Our semi-supervised learning framework for RGB-D object recognition. Firstly, we extract features to represent the RGB and depth view of each object respectively. Then we employ co-training to iteratively learn from the unlabeled data using the two distinct feature sets. In the figure, TC means triangular coding, PP means pyramid pooling, SC means sparse coding (see Section 2.3 for details).

88 to the unsupervised deep learning model to address the problem of cropping or  
 89 warping. The core idea is inspired from the pioneer work [29], which utilized  
 90 SPM layer in the supervised deep learning model and yielded impressive results.

- 91 • Analyse and Evaluate most representative RGB-D features in an unbiased way  
 92 by utilizing four data modalities, including RGB, grayscale, depth and surface  
 93 normals, which can provide a meaningful guideline how to best represent the  
 94 new RGB-D data.

95 The rest of this paper is organized as follows: Section 2 proposes our semi-supervised  
 96 learning framework for RGB-D object recognition, including the semi-supervised learn-  
 97 ing method based on co-training, the feature CNN-SPM-RNN, and a unified framework  
 98 for feature evaluation. Section 3 empirically evaluates and ranks all the representative  
 99 features in an unbiased way, and shows the comparison of our semi-supervised method  
 100 with the state of the arts on several public RGB-D object databases. Finally, Section 4  
 101 concludes the paper and discusses the future work.

## 102 2. Our Semi-supervised Framework

103 As shown in Fig. 2, our semi-supervised learning framework is proposed for RGB-  
 104 D object recognition. There are three modules in the framework: (1) feature representa-  
 105 tion for the RGB view; (2) feature representation for the depth view; and (3) exploiting  
 106 co-training to utilize a small set of labeled data and large amount of unlabeled data.

107 The core idea of the framework is to improve the two classifiers trained on the two  
 108 distinct feature sets iteratively by co-training. Thus how to extract effective feature  
 109 representation for each view is the fundamental step.

110 In the following subsections, we first prove that co-training can succeed in learning  
 111 from unlabeled RGB-D examples, and propose the co-training algorithm for RGB-D  
 112 object recognition. Then we introduce our feature CNN-SPM-RNN, followed by a  
 113 unified framework to evaluate recent state-of-the-art features for RGB-D objects.

### 114 2.1. Semi-supervised Learning

115 We employ co-training as our semi-supervised learning method to learn from the  
 116 unlabeled RGB-D data, as shown in Fig. 2. Firstly, Two assumptions to guarantee  
 117 the success of learning with co-training are introduced. Then a specific co-training  
 118 algorithm for RGB-D object recognition is proposed.

#### 119 2.1.1. Theoretical Assumptions

120 Some notations are given as follows: Let  $D$  denote the distribution over the feature  
 121 space  $F = F_1 \times F_2$ , where  $F_1$  and  $F_2$  correspond to two different views of an example.  
 122 Assume  $F^+$  and  $F^-$  are the positive and negative regions of  $F$  respectively (for sim-  
 123 plicity we consider binary classification here), and Let  $c$  be the target function. Then  
 124 for  $i \in \{1, 2\}$ , we define  $F_i^+ = \{f_i \in F_i : c_i(f_i) = 1\}$  and  $F_i^- = F_i - F_i^+$ . In order  
 125 to bootstrap co-training, a initial labeled set for the two views  $S_1^0 \subseteq F_1^+$  and  $S_2^0 \subseteq F_2^+$   
 126 are provided. During the iterative learning procedure of co-training, a hypothesis  $h_i$  is  
 127 devised as a subset of  $F_i$ , where  $f_i \in h_i$  means that  $h_i$  is confident that  $f_i$  is positive,  
 128 and  $f_i \notin h_i$  means that  $h_i$  has no opinion.

129 The research [24] proved it was sufficient for co-training to succeed, when given  
 130 the two assumptions on the underlying data distribution:

- 131 • The learning algorithm for each view is able to learn from positive data only.
- 132 • The marginal distribution  $D^+$  is  $\epsilon$ -expanding ( $\epsilon > 0$ ).

133 The first assumption means that,  $\forall D_i^+$  over  $F_i^+$ , given access to examples from  $D_i^+$ ,  
 134 each learning algorithm is able to produce a hypothesis  $h_i$  such that  $Pr(error_{D_i^+}(h_i) \leq$   
 135  $\epsilon) \geq 1 - \delta$ , where  $\epsilon, \delta > 0$ . This can be thought of as predicting the examples either  
 136 “positive with confidence” or “has no opinion”. According to [24], this assumption is  
 137 easy to fulfill in practice if the positive class is cohesive and the negative class is not;

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**Algorithm 1** Co-Training Algorithm for RGB-D Object Recognition

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**Input:**

$\mathbf{F}_{\text{RGB}}$ : RGB feature set;  $\mathbf{F}_{\text{depth}}$ : depth feature set;  
 $\theta_{\text{RGB}}$ : a confidence threshold for RGB feature set;  
 $\theta_{\text{depth}}$ : a confidence threshold for depth feature set;  
 $\mathbf{L}$ : labeled pool;  $\mathbf{U}$ : unlabeled pool;  
 $\mathbf{I}$ : the maximum number of iteration rounds

**Output:**

$\mathbf{C}_{\text{RGB}}$ : RGB classifier;  $\mathbf{C}_{\text{depth}}$ : depth classifier  
1:  $i \leftarrow 0$ ;  
2: **repeat**  
3:  $\mathbf{C}_{\text{RGB}} \leftarrow \text{train}(\mathbf{F}_{\text{RGB}}, \mathbf{L})$ ;  
4:  $\mathbf{C}_{\text{depth}} \leftarrow \text{train}(\mathbf{F}_{\text{depth}}, \mathbf{L})$ ;  
5:  $\mathbf{C}_{\text{RGB}} \rightarrow \text{predict}(\mathbf{F}_{\text{RGB}}, \mathbf{U})$ , for each predicted class  $c_j$ , choose  $|n_j|$  most confident examples and add them to  $\mathbf{L}$ ,  $\forall n_j, \text{Score}(n_j) \geq \theta_{\text{RGB}}$ ;  
6:  $\mathbf{C}_{\text{depth}} \rightarrow \text{predict}(\mathbf{F}_{\text{depth}}, \mathbf{U})$ , for each predicted class  $c_j$ , choose  $|n_j|$  most confident examples and add them to  $\mathbf{L}$ ,  $\forall n_j, \text{Score}(n_j) \geq \theta_{\text{depth}}$ ;  
7:  $i++$ ;  
8: **until**  $i > \mathbf{I}$  or  $\mathbf{U}$  is empty  
9: **return**  $\mathbf{C}_{\text{RGB}}$  and  $\mathbf{C}_{\text{depth}}$ ;

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138 The second assumption can be interpreted as the following definition:

139 **Definition**  $D^+$  is  $\epsilon$ -expanding if for any  $S_1 \subseteq F_1^+$ ,  $S_2 \subseteq F_2^+$ , we have

$$\Pr(S_1 \oplus S_2) \geq \epsilon \min [\Pr(S_1 \wedge S_2), \Pr(\bar{S}_1 \wedge \bar{S}_2)].$$

140 where  $\Pr(S_1 \wedge S_2)$  denotes the probability mass on examples that are confidently pre-  
141 dicted as positive region by both views, and  $\Pr(S_1 \oplus S_2)$  denotes the probability mass  
142 on examples for which we are confident about just one view. Note that  $\epsilon$ -expanding  
143 is necessary to guarantee co-training will succeed, because if  $S_1$  and  $S_2$  are confident  
144 sets and do not expand, then we might never see the expected situation that examples  
145 for one hypothesis could help the other.

### 146 2.1.2. Co-training Algorithm

147 An intuitive interpretation of co-training is as follows: Firstly, two initial classifiers  
148 over the respective views are trained on a small labeled sample. Then each classifier is  
149 used to label the confident examples for the other classifier, for which these examples  
150 can be seen as random training instances. In this case, each classifier can benefit from  
151 the additional examples by the other one and improve its classification accuracy in  
152 every rounding training.

153 We propose our co-training algorithm for RGB-D object recognition (multi-class

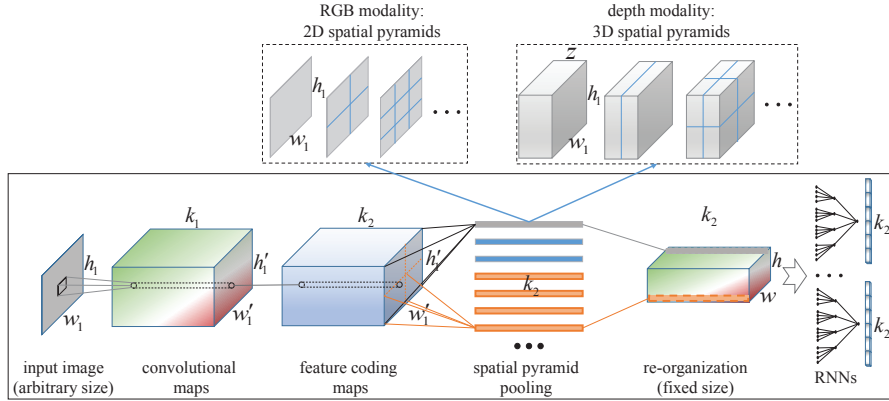


Figure 3: An overview of the feature learning structure of CNN-SPM-RNN. The SPM layer in this paper consists of feature coding, spatial pyramid pooling, and re-organization, which can input convolution feature maps with arbitrary sizes (e.g.,  $w'_1 \times h'_1 \times k_1$ , where  $w'_1 \times h'_1$  is the size of each feature map, and  $k_1$  is the number of feature maps), and then output fixed-scale feature maps (i.e.,  $w$ ,  $h$  and  $k_2$  are fixed to the same for all inputs).

154 classification) in Algorithm 1. Firstly, we extract feature representations  $F_{RGB}$  and  
 155  $F_{depth}$  for the RGB and depth view respectively. Then we train two linear SVM classi-  
 156 fiers  $C_{RGB}$  and  $C_{depth}$  based on a small set of initial labeled examples  $L$  using the two  
 157 feature sets.  $C_{RGB}$  and  $C_{depth}$  are applied to predict the examples from the unlabeled  
 158 training sets  $U$  separately. For each classifier,  $|n_j|$  most confidently predicted instances  
 159 of each class whose scores are higher than a threshold will be transferred from  $U$  to  $L$   
 160 in every iteration. Generally, we assign  $|n_j|$  a small value and keep it the same for all  
 161 the classes. The algorithm runs until the iteration number reaches the given maximum  
 162 threshold or all the unlabeled examples in  $U$  are labeled. The outputs of the algorithm  
 163 are the updated classifiers  $C_{RGB}$  and  $C_{depth}$ .

164 At the inference time,  $C_{RGB}$  and  $C_{depth}$  are combined to predict the category of  
 165 the given example based on their classification scores:

$$c = \arg_{c_i \in \chi} \text{Max}(\alpha S_{C_{RGB}}^{c_i} + (1 - \alpha) S_{C_{depth}}^{c_i}) \quad (1)$$

166 where  $\chi$  is the label set of all the categories,  $S_{C_{RGB}}^{c_i}$  and  $S_{C_{depth}}^{c_i}$  are predicted scores  
 167 of category  $c_i$  for an given example, and  $\alpha$  is the coefficient to control the contribution  
 168 of each view.

## 169 2.2. CNN-SPM-RNN

170 CNN-SPM-RNN is built on the unsupervised feature learning structure of CNN-  
 171 RNN [4]. CNN-RNN mainly consists of three steps: resizing all the images to the



172 same scale, extracting low level feature for each image by a single convolutional lay-  
 173 er, and finally applying multiple fixed-tree RNNs to learn high order feature repre-  
 174 sentation based on the low level feature responses. Although CNN-RNN can learn  
 175 powerful features from the raw data, such artificial processing of the first step, i.e.,  
 176 resizing all the images to the same scale by simply cropping or warping the images,  
 177 may degrade the performance of the learned features. In order to adopt CNN-RNN  
 178 model for images of arbitrary sizes, we replace the first step of CNN-RNN by a SPM  
 179 layer, which is composed of three steps: feature coding, spatial pyramid pooling and  
 180 re-organization, as showed in Fig. 3. To fairly compare CNN-SPM-RNN with CNN-  
 181 RNN, the parameters of the single-layer CNN and multiple RNNs are kept the same  
 182 as the work [4], i.e.,  $k_1 = 128$  filters with  $9 \times 9$  size are learned for the single-layer  
 183 CNN, the input fixed-scale feature maps for each RNN are  $27 \times 27 \times 128$ -dimensional  
 184 ( $w = 27, h = 27, k_2 = 128$ ). Now we describe the details of each step of the proposed  
 185 SPM layer.

**Feature Coding.** The goal is to learn high-level local features to represent ob-  
 jects more powerfully, compared with the low-level convolutional descriptors. First, a  
 codebook  $\{c_1, c_2, \dots, c_{k_2}\}$  ( $k_2 = 128, c_i \in \mathbb{R}^{k_1=128}$ ) is learned by k-means cluster-  
 ing over the sampled convolutional descriptors. Second, each convolutional descriptor  
 $x \in \mathbb{R}^{k_1=128}$  is encoded by the codebook with triangular voting [33]:

$$\begin{aligned}
 f(x) &= (f_{c_1}(x), f_{c_2}(x), \dots, f_{c_{k_2}}(x)), \\
 \text{s.t. } f_{c_i}(x) &= \max(0, \mu - \|x - c_i\|_2^2), \\
 \mu &= \frac{1}{k_2} \sum_{i=1}^{k_2} \|x - c_i\|_2^2.
 \end{aligned} \tag{2}$$

186 where  $f(x) \in R^{k_2=128}$ .

187 **Spatial Pyramid Pooling.** 2D and 3D spatial pyramid pooling are employed for  
 188 the RGB and depth modality, respectively. For the 2D spatial pyramid pooling, the  
 189 partitions are constrained in the two-dimensional image space. While for the 3D spa-  
 190 tial pyramid pooling, the partitions are performed in the three-dimension depth space.  
 191 See Fig. 3 for an intuitive understanding. The work [34] also showed that 3D spatial  
 192 pyramids were necessary to represent the depth modality. In this paper, we set the  
 193 number of the pyramid bins as  $27 \times 27 = 729$ , in order to obtain the same size of the  
 194 fixed-scale feature maps as [4] for a fair comparison. For each bin, max pooling is used  
 195 to aggregate the neighboring features to a 128-dimensional feature vector.

196 **Re-Organization.** After spatial pyramid pooling, the convolutional responses with  
197 arbitrary sizes are transformed to a fixed number of feature vectors. We re-organize  
198 all the feature vectors to a 3D feature map ( $\in \mathbb{R}^{27 \times 27 \times 128}$ ) with a fixed order. Finally,  
199 the 3D feature map is input to multiple RNNs to learn the global feature representation  
200 as [4].

201 We employ CNN-SPM-RNN to extract features for each modality of RGB (2D  
202 spatial pyramids), grayscale (2D spatial pyramids), depth (3D spatial pyramids) and  
203 surface normals (2D spatial pyramids), respectively. For each object, the RGB feature  
204 and grayscale feature are concatenated to represent the appearance information, while  
205 depth feature and surface normal feature are combined to capture shape cues.

### 206 2.3. Feature Analysis and Evaluation

207 Various features have already been developed for RGB-D object recognition. In this  
208 section, we introduce four state-of-the-art features: kernel descriptors (KDES) [1], con-  
209 volutional k-means descriptors (CKM) [2], hierarchical matching pursuit (HMP) [3],  
210 and convolutional-recursive neural networks (CNN-RNN) [4], which are more discrim-  
211 inative and robust than the popular orientation histogram features, such as SIFT [35]  
212 and spin images [36]. In order to compare these features with the CNN-SPM-RNN,  
213 we analyse the characteristics of them first, and then propose a unified framework to  
214 extract all these features effectively for an unbiased evaluation.

#### 215 2.3.1. Feature Analysis

216 The four representative features: KDES [1], CKM [2], HMP [3] and CNN-RNN [4],  
217 employ very different methods to extract features from the raw data, compared to the  
218 handcrafted features utilized in the baseline work [6]. Furthermore, they take advan-  
219 tage of different data modalities among RGB images, grayscale images, depth maps  
220 and surface normals to capture cues for object recognition, as shown in Table 1. The  
221 analysis of the above features is shown as follows:

222 The baseline work [6] extracts **a set of handcrafted features** to represent the two  
223 distinct views of RGB-D objects. To capture the visual appearance of the RGB view,  
224 they extract SIFT descriptors over grayscale images, texton histograms [37] and color  
225 histograms over the RGB images. The shape of the depth view is represented by spin  
226 images computed from depth maps and surface normals. Regardless of their effective-  
227 ness, these well tuned handcrafted features are hard to design and only can capture a

Features	RGB View		Depth View	
	RGB	Grayscale	Depth	Surface Normals
Handcrafted features [6]	✓	✓	✓	✓
KDES [1]	✓	✓	✓	✓
CKM [2]	✓	–	✓	–
HMP [3]	✓	✓	✓	✓
CNN-RNN [4]	✓	–	✓	–
CNN-SPM-RNN	✓	✓	✓	✓

Table 1: Different data modalities are exploited to capture cues for object recognition for different methods. Generally, RGB and grayscale images can capture visual appearance of the RGB view, while depth maps and surface normals can capture shape information of the depth view.

228 small set of recognition cues from raw data. For example, SIFT is able to capture some  
229 sort of edge information while ignores color information; Spin images are extended  
230 to 3D objects analogous to SIFT over 2D images, but also has limited capability to  
231 capture useful shape or geometry information.

232 **KDES [1]** provides a generalized way to extend orientation histogram features like  
233 SIFT to a broad class of similar feature patterns. The previous work [38] has already  
234 shown that the well-designed SIFT features are equivalent to a certain type of match  
235 kernel over image patches. Thus, it is very convenient to design a set of kernel descrip-  
236 tors on top of various attributes, including 3D shape, physical size, edges, gradients,  
237 etc.

238 **CKM [2]** adapts single-layer feature learning networks based on k-means clus-  
239 tering for 2D images [33] to RGB-D data. To keep the feature learning process as  
240 effective as [33], CKM takes the depth channel as the fourth channel of the RGB chan-  
241 nels and directly learns features from the four channels. By using the state-of-the-art  
242 image pre-processing and feature encoding of [33], CKM can obtain useful transla-  
243 tional invariance of low-level features from raw data such as edges, and can be robust  
244 to small deformations of objects. However, without information of grayscale images  
245 and surface normals, the performance of CKM is restricted a lot for object recognition.

246 **HMP [3]** constructs a two-layer architecture to generate features over complete  
247 RGB-D images based on sparse coding. It can discover low-level structures such as  
248 edges at the first layer, and high-level structures such as shapes and object parts at the  
249 second layer. HMP learns features from each data modality, then combines the RGB

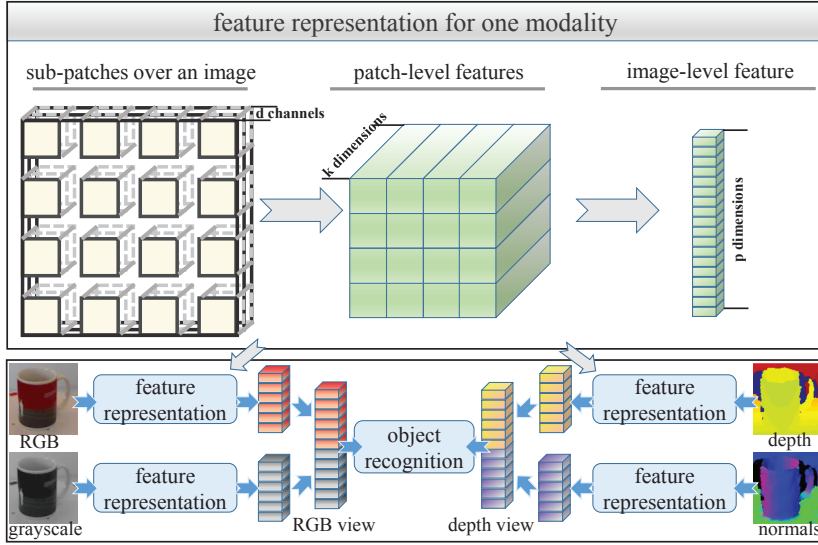


Figure 4: A unified framework to represent the RGB and depth view of RGB-D objects. For each type of features, we extract them from four data modalities, respectively. Then combine the RGB and grayscale features to capture visual appearance of the RGB view, and the depth and normal features to capture shape of the depth view.

250 and grayscale features to represent the visual appearance of the RGB view, and captures  
 251 the shape cues by concatenating the depth and surface normal features.

252 **CNN-RNN [4]** is a deep feature learning model based on a combination of con-  
 253 volutional and recursive neural networks. The single CNN layer can learn low-level  
 254 translationally invariant features which are assembled by multiple RNNs [28] to con-  
 255 struct high order representation. Similar to CKM, CNN-RNN only makes use of RGB  
 256 images and depth maps for object recognition.

257 Both the baseline work and KDES utilize manually designed features, while CK-  
 258 M, HMP, CNN-RNN and CNN-SPM-RNN belong to unsupervised feature learning  
 259 methods.

### 260 2.3.2. Unbiased Feature Evaluation

261 To obtain an unbiased evaluation for all the above features, we propose a unified  
 262 framework to represent RGB-D objects by adapting them to the four data modalities, as  
 263 shown in Fig. 4. For each type of features, the RGB and grayscale images are used to  
 264 capture visual appearance of the RGB view, and the depth and surface normal images  
 265 are exploited to capture shape cues of the depth view. We can obtain more powerful  
 266 view representation by utilizing additional information of grayscale and surface nor-  
 267 mals, compared to those only based on RGB and depth in their original papers.

268 Specifically, we are capable of extracting CKM descriptors from each data modali-  
269 ty respectively following the same process of [2] over RGB-D images. Then, we learn  
270 the image-level features for each data modality using a bag-of-words model with spa-  
271 tial pyramid pooling [30]. Finally, following the framework, CKM features from the  
272 four data modalities will be combined to represent the RGB view and depth view re-  
273 spectively. To distinguish our CKM features from the original paper [2], we call them  
274 **enhanced CKM**; Similarly, we employ CNN-RNN to learn features not only from the  
275 RGB and depth images but also from the grayscale and surface normal images. Then  
276 the RGB and grayscale features are combined to describe the RGB view, while the  
277 depth and surface normal features are concatenated to represent the depth view. We  
278 call our CNN-RNN features **enhanced CNN-RNN**. Since the baseline work, KDES,  
279 HMP and CNN-SPM-RNN have already taken advantage of the four data modalities  
280 for object recognition, we keep them the same with the original papers.

### 281 3. Experiments

282 Our experiments are carried out on three publicly available RGB-D object datasets.  
283 On the first challenging Washington RGB-D Object Database [6], we evaluate all the  
284 representative features in an unbiased way and compare the performance of the pro-  
285 posed semi-supervised method with the state of the arts. On the other two datasets,  
286 we further verify the effectiveness of the semi-supervised learning method. All the  
287 experimental codes including the introduced features and the semi-supervised learning  
288 method are released at the website <http://www.openpr.org.cn/>.

289 We follow the unified framework in Section 2.3.2 to extract all the introduced fea-  
290 tures for the RGB view (RGB + grayscale) and the depth view (depth + normals). The  
291 experimental settings of each feature extraction method are as follows:

292 **KDES**: To construct image-level features for each kind of kernel descriptors, we  
293 follow the process of [1] to obtain high performance, which considers  $[1 \times 1, 2 \times 2, 3 \times 3]$   
294 pyramid subregions, and use EMK [39] with 500 basis vectors learned by k-means on  
295 400,000 kernel descriptors sampled from training images. The resulting dimensionali-  
296 ty per kernel descriptor based image representation is  $(1 + 4 + 9) \times 500 = 7000$ , then  
297 reduced to 1000 using principal component analysis.

298 **Enhanced CKM**: To guarantee the feature learning method effective and success-  
299 ful as [2], a bag-of-words model is exploited to construct image-level features for the

300 CKM descriptors extracted from each data modality. We learn 1000 codewords us-  
 301 ing k-means on 400,000 descriptors and use average pooling with spacial pyramids  
 302  $[1 \times 1, 2 \times 2, 3 \times 3]$  to compute the feature responses. The final dimensionality of per  
 303 image-level feature representation is 14,000.

304 **HMP:** HMP can directly learn the image-level features from each data modality.  
 305 Note that we only aggregate the responses of the patch features at the second layer  
 306 instead of a jointly pooling [3], because the dimensionality of the jointly pooling is  
 307 up to 36,050 (grayscale, depth) or 58,100 (RGB, normals) per object, which requires  
 308 too much memory and computing time. Our processing can reduce the dimension-  
 309 ality of all the four modalities' representations to 7,000 and can obtain approximate  
 310 performance.

311 **Enhanced CNN-RNN:** Similar to [4], for each data modality (resized to the fixed-  
 312 scale, e.g.,  $148 \times 148$ ), we learn 128 filters by k-means clustering over the patches, and  
 313 use 64 randomly initialized RNNs to compose the convolutional responses to the final  
 314 image representation with  $128 \times 64 = 8192$  dimensions.

315 **CNN-SPM-RNN:** CNN-SPM-RNN is proposed to extract powerful features from  
 316 the raw data (without cropping or warping). For a fair comparison, the parameters  
 317 of the single-layer CNN and multiple RNNs are kept the same with the CNN-RNN  
 318 model [4]. Similarly, to obtain the same size of the fixed-scale feature map, the size of  
 319 the codebook is set to  $k_2 = 128$ , and the number of the pyramid bins is set to  $27 \times 27 =$   
 320 729. Since there are a lot of selectable ways to partition the image to collect the equal  
 321 number of bins, we simply choose one without fine-tuning. The configurations are  
 322 given below.

323 2D spatial pyramids:  $\{3 \times 3, 8 \times 8, 16 \times 16, 20 \times 20\}$

3D spatial pyramids:

$\{1 \times 1 \times 1, 1 \times 1 \times 2, 1 \times 1 \times 4, 1 \times 1 \times 8, 1 \times 1 \times 16, 1 \times 1 \times 32, 1 \times 1 \times 36,$

$1 \times 3 \times 1, 1 \times 3 \times 2, 1 \times 3 \times 4, 1 \times 3 \times 8, 1 \times 3 \times 16, 1 \times 3 \times 32,$

$3 \times 1 \times 1, 3 \times 1 \times 2, 3 \times 1 \times 4, 3 \times 1 \times 8, 3 \times 1 \times 16, 3 \times 1 \times 32,$

$2 \times 2 \times 1, 2 \times 2 \times 2, 2 \times 2 \times 4, 2 \times 2 \times 8, 2 \times 2 \times 16, 2 \times 2 \times 32\}$ .

324 Finally, the re-organization 3D feature map of each modality of each object is input  
 325 into the fixed-tree RNNs, and composed to the global feature representation with  $128 \times$   
 326  $64 = 8192$  dimensions.

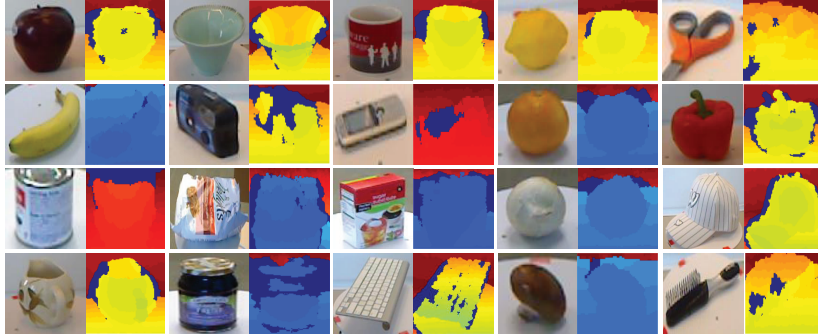


Figure 5: Object examples from the Washington RGB-D object database. Each object (RGB + depth) shown here belongs to a different category.

### 3.1. Washington RGB-D Object Database

The first experimental database is a large-scale hierarchical multi-view RGB-D object dataset [6]. The database consists of a total of 207,920 RGB-D images containing 300 physically distinct everyday object instances (see Fig. 5). All the instances are grouped into 51 categories. Each object instance is imaged from three viewing heights ( $30^\circ$ ,  $45^\circ$  and  $60^\circ$  above the horizon) while it rotates on a turntable, resulting in roughly 600 images per instance. We subsample every 5th frame for each instance and reduce the size of the total database to 41,877 RGB-D images.

This paper focuses on category recognition. The dataset settings for supervised learning and our semi-supervised learning are given as below: (1) for supervised learning, we follow the setting in [6], which provides 10 random splits to generate training and test sets from the database. For each split, one object instance is selected randomly from each category for testing and all remaining object instances are for training, resulting in around 35,000 training examples and 6,877 test examples. Note that all training sets are labeled for supervised learning; (2) for our semi-supervised learning, the main setting is the same as the supervised learning, but the training set is randomly divided into two parts: labeled and unlabeled examples, e.g., if we label 20% of the training set, we get around 7,000 labeled and 28,000 unlabeled for the training set. Note that the learning process of co-training is based on the labeled and unlabeled examples of the training set. All the experiments are repeated 10 times on the test set and the average accuracies are given.

Methods	Labeled Size	Depth	RGB	Combine
Linear SVM [6]	35k	$53.1 \pm 1.7$	$74.3 \pm 3.3$	$81.9 \pm 2.8$
Kernel SVM [6]	35k	$64.7 \pm 2.2$	$74.5 \pm 3.1$	$83.8 \pm 3.5$
Random Forest [6]	35k	$66.8 \pm 2.5$	$74.7 \pm 3.6$	$79.6 \pm 4.0$
IDL [19]	35k	$70.2 \pm 2.0$	$78.6 \pm 3.1$	$85.4 \pm 3.2$
3D SPMK(L=2) [34]	35k	67.8	–	–
KDES [1]	35k	$78.8 \pm 2.7$	$77.7 \pm 1.9$	$86.2 \pm 2.1$
CKM [2]	35k	–	–	$86.4 \pm 2.3$
original HMP [40]	35k	$70.3 \pm 2.2$	$74.7 \pm 2.5$	$82.1 \pm 3.3$
HMP [3]	35k	$81.2 \pm 2.3$	$82.4 \pm 3.1$	$87.5 \pm 2.9$
CNN-RNN [4]	35k	$78.9 \pm 3.8$	$80.8 \pm 4.2$	$86.8 \pm 3.3$
CNN-RNN+CT [32]	7k	$77.7 \pm 1.4$	$81.8 \pm 1.9$	$87.2 \pm 1.1$
enhanced CNN-RNN+CT	7k	$82.0 \pm 2.1$	$84.1 \pm 1.3$	$89.9 \pm 1.3$
CNN-SPM-RNN+CT	7k	<b><math>83.6 \pm 2.3</math></b>	<b><math>85.2 \pm 1.2</math></b>	<b><math>90.7 \pm 1.1</math></b>

Table 2: Comparison of recent results on the Washington RGB-D object database. CT means the proposed semi-supervised learning method with co-training.

### 3.1.1. Comparison to the state-of-the-art

We compare the results of our semi-supervised learning method to the recent methods, as shown in Table 2. For semi-supervised learning, we only label 20% of the training set, and exploit the enhanced CNN-RNN and CNN-SPM-RNN to extract RGB-D features, respectively. We utilize linear SVMs to train the two classifiers, and set  $\alpha = 0.65$ ,  $I = 500$  in Equation 1 when combine the two classifiers to predict the test set. The results demonstrate that our method can achieve the state-of-the-art performance against other methods. Furthermore, the CNN-SPM-RNN features are more discriminative than the enhanced CNN-RNN features, showing the effectiveness of maintaining the natural data sizes and aspect ratios by the SPM layer.

Among all these methods, the previous work [32] also employs semi-supervised learning method for RGB-D object recognition. However, The work [32] only extracts features from RGB images and depth images based on the CNN-RNN model [4], without considering grayscale images and surface normals. The experimental results also demonstrate the recognition performance can be improved with the additional information provided by grayscale and surface normals.

### 3.1.2. Unbiased Feature Evaluation in Supervised Setting

Since the two distinct feature sets  $F_{RGB}$  and  $F_{depth}$  are crucial for our semi-supervised learning, it’s very necessary for us to fairly evaluate different features and choose the best one. Firstly, we give unbiased feature evaluation in supervised setting:



Methods	Depth	RGB	Combine
KDES [1]	$78.8 \pm 2.7$	$77.7 \pm 1.9$	$86.2 \pm 2.1$
enhanced CKM	$82.8 \pm 2.4$	$81.8 \pm 2.7$	$87.5 \pm 2.4$
HMP [3]	$81.2 \pm 2.3$	$82.4 \pm 3.1$	$87.5 \pm 2.9$
enhanced CNN-RNN	$82.4 \pm 2.3$	$84.8 \pm 1.4$	$89.9 \pm 1.4$
CNN-SPM-RNN	<b><math>83.4 \pm 2.4</math></b>	<b><math>85.4 \pm 1.3</math></b>	<b><math>90.7 \pm 1.4</math></b>

Table 3: Unbiased feature evaluation in supervised setting. Here all the training examples of size 35k are labeled, and linear SVM is used as our classifier.

368 All the five feature extraction methods are exploited to represent the RGB-D objects  
369 respectively as introduced in Section 2.3, and linear SVMs are used as our classifiers.  
370 We set  $\alpha = 0.65$  when combine the two classifiers  $C_{RGB}$  and  $C_{depth}$  to recognize  
371 objects. The results are shown in Table 3.

372 It is worth to note that the ranking results in our evaluation are quite different from  
373 the published results. As shown in Table 2, the published results are ranked as fol-  
374 lows: KDES < CKM < CNN-RNN < HMP. However, the capabilities of CKM and  
375 CNN-RNN are restricted a lot since grayscale images and surface normals are ignored  
376 in [2, 4]. The reasonable ranking results in our unbiased feature evaluation in Table 3  
377 are: KDES < enhanced CKM, HMP < enhanced CNN-RNN. It can be analysed that  
378 kernel descriptors are a set of generalized histogram features like SIFT, although differ-  
379 ent kernel descriptors can be designed to capture different cues of objects, this kind of  
380 handcrafted features still have limited capability to describe an object; Both enhanced  
381 CKM and HMP are unsupervised feature learning models, which can learn more pow-  
382 erful features from the raw data than a set of manually designed kernel descriptors. The  
383 unsupervised learning structure can learn translational invariance of low-level features  
384 (the first layer in enhanced CKM and HMP) as well as some sort of high-level struc-  
385 tures (the second layer of HMP) from the raw data. The enhanced CNN-RNN performs  
386 better, which employs a deep feature learning structure to discover discriminative and  
387 robust features. Our CNN-SPM-RNN achieves the state-of-the-art performance. Ex-  
388 perimental results imply that CNN-SPM-RNN features are of the highest probability  
389 to guarantee the success of co-training in learning from the unlabeled RGB-D data.

### 390 3.1.3. Unbiased Feature Evaluation in Semi-supervised Setting

391 The same experiments are executed in the semi-supervised setting. Similarly, we  
392 extract the five features as the unified framework in Section 2.3, then exploit co-training

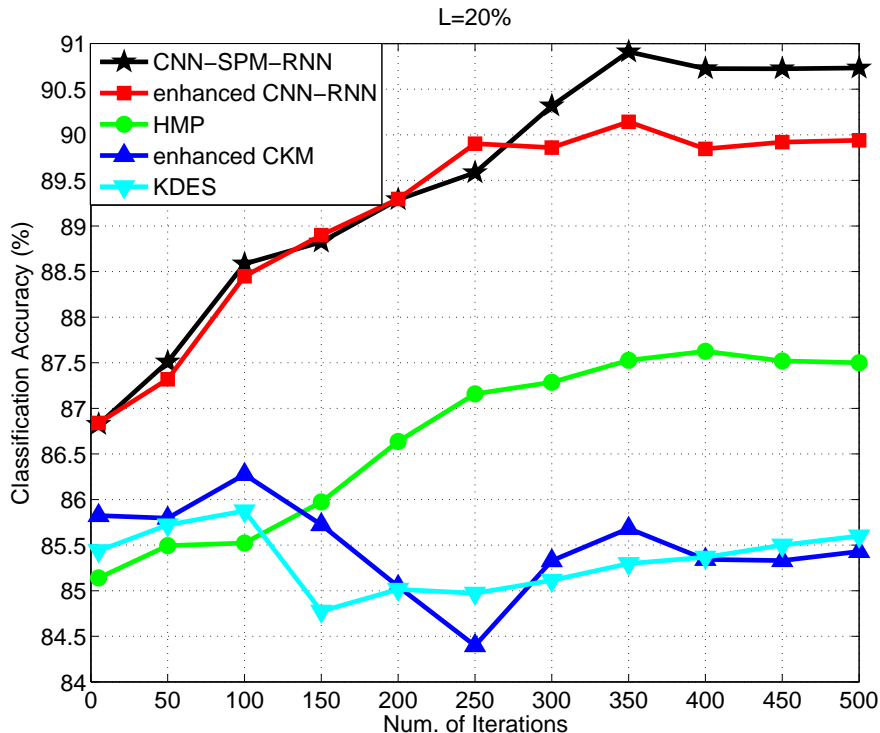


Figure 6: Unbiased feature evaluation in semi-supervised learning. We only label 20% (around 7k) of the training set, and use linear SVM as our classifiers. In the figure, we only report the combined results on the testing set.

393 to iteratively improve the two linear SVM classifiers through learning from the unlabeled data. In the learning process, we set  $|n_j| = 2$  for each predicted class. We 394 combine the two classifiers to predict the testing set and give the recognition accuracy 395 every 50 iterations, as shown in Fig 6. 396

397 Among the five kinds of features, only CNN-SPM-RNN, enhanced CNN-RNN and 398 HMP can make co-training succeed in learning from the unlabeled RGB-D data. The 399 reason is that the two classifiers  $C_{RGB}$  and  $C_{depth}$  based on CNN-SPM-RNN, en- 400 hanced CNN-RNN or HMP features can be reliable to learn from the unlabeled data in 401 each iteration, i.e., most examples transferred from the unlabeled pool  $U$  to the labeled 402 pool  $L$  are correctly labeled. However,  $C_{RGB}$  and  $C_{depth}$  based on kernel or enhanced 403 CKM features could add many examples from the unlabeled pool  $U$  with incorrect labels, 404 which can in turn degrade the performance of the two classifiers. The rationale 405 behind this result is that the features extracted by shallow learning models (enhanced 406 CKM: one layer, KDES: manually designed) are not as robust as the deeper learning 407 models (HMP: two layers, enhanced CNN-RNN and CNN-SPM-RNN: multiple lay-

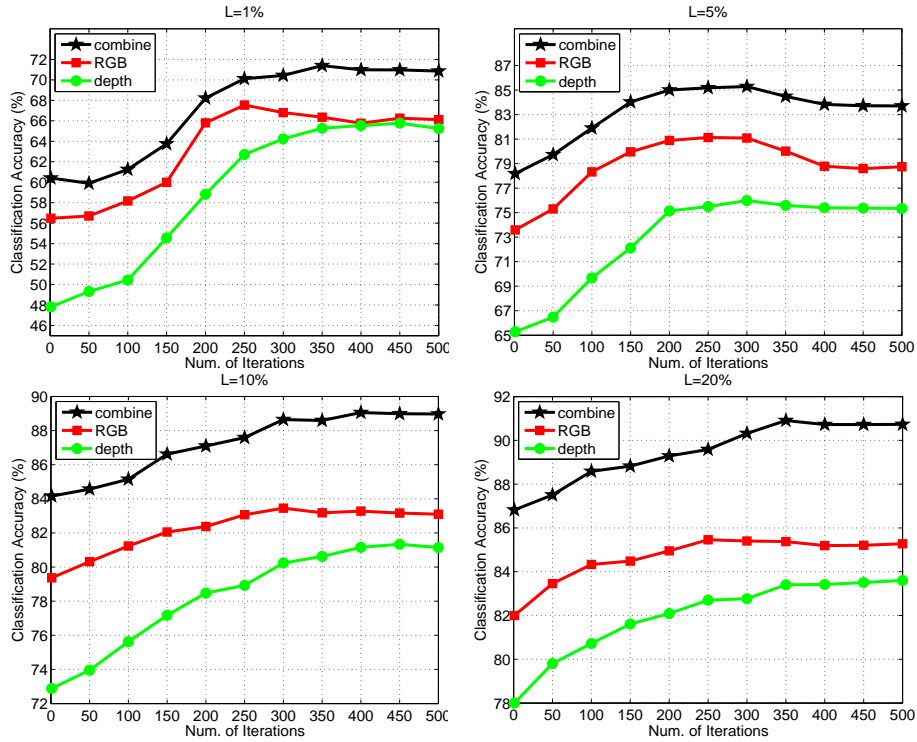


Figure 7: Recognition accuracy with iteration number  $I$  and the labeled size  $L$  ( $|n_j| = 2, \alpha = 0.65$ ).

408 ers.) The biggest difference between the semi-supervised learning and the supervised  
 409 learning, is that enhanced CKM performs much worse than HMP. It is probable that  
 410 the features learned by the two-layer learning structure of HMP can obtain more ro-  
 411 bustness and generalization ability than one-layer enhanced CKM features. As well,  
 412 CNN-SPM-RNN performs the best in our semi-supervised learning.

### 413 3.1.4. Parameter Analysis

414 In this section, first, we analyse the effectiveness of the CNN-SPM-RNN feature  
 415 learning model. Second, using the CNN-SPM-RNN model with default setting to ex-  
 416 tract features, we analyse the effectiveness of the co-training model.

417 **CNN-SPM-RNN.** CNN-SPM-RNN model is proposed to address the problem of  
 418 cropping or warping in CNN-RNN model, and learn more powerful features from the  
 419 raw data. Besides spatial pyramid pooling, the success of CNN-SPM-RNN is highly  
 420 dependent on the feature coding layer as well as its codebook size.

421 (1) CNN-SPM-RNN with and without feature coding layer. Fig. 8 (a) shows that  
 422 a feature coding layer can significantly improve the performance of the learned fea-

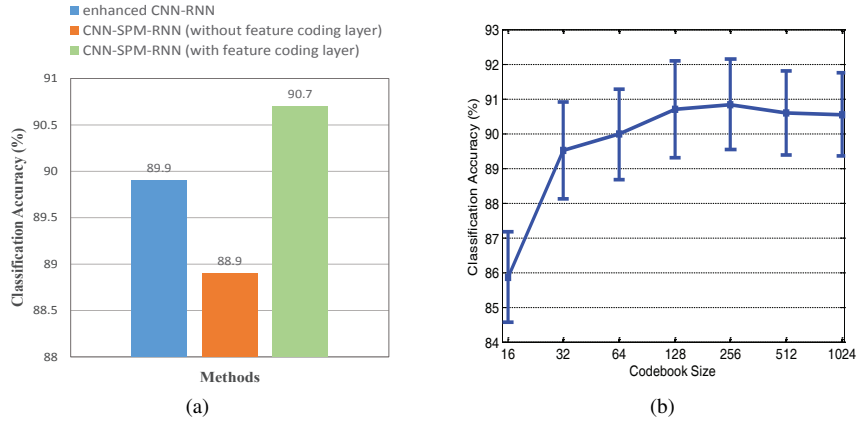


Figure 8: (a) Performance of CNN-SPM-RNN with feature coding layer ( $k_2 = 128$ ) and without feature coding layer; (b) Performance of CNN-SPM-RNN with the codebook size of the feature coding layer. For both (a) and (b), the classification accuracy is based on the supervised setting.

423 tures. Through feature coding, we can learn high-level feature responses based on the  
 424 low-level convolutional responses, which can further improve the effectiveness of the  
 425 learned features. This is also one of the main differences between our work (for unsu-  
 426 pervised deep learning model) and He et al’s work [29] (for supervised deep learning  
 427 model), when applying spatial pyramid pooling to adopt the feature learning model for  
 428 arbitrary image sizes.

429 (2) Influence of the codebook size of the feature coding layer. Fig. 8 (b) demon-  
 430 strates that the performance of the CNN-SPM-RNN feature can rapidly grow with larg-  
 431 er codebook size at the beginning. When the codebook size  $k_2 > 128$ , the recognition  
 432 accuracy keeps stable with a very high value. The main reason is that more codewords  
 433 can describe more patterns of features for object recognition, while some mild over-  
 434 fitting can exist for very large codebook size. Considering the efficiency and accuracy,  
 435  $k_2 = 128$  is used for CNN-SPM-RNN.

436 **Co-training.** Using CNN-SPM-RNN model to extract features for each modality  
 437 of each object, the co-training method is closely related to the iteration number  $I$ , the  
 438 labeled training size  $L$ , the number of added examples  $|n_j|$ , and the coefficient  $\alpha$ . We  
 439 analyze each by fixing other parameters in the following.

440 (1) Influence of the number of iterations. As shown in Fig. 7, all the accuracy  
 441 curves of co-training from  $L = 1\%$  to  $L = 20\%$  suggest the similar trends as the  
 442 number of iterations increases. After several hundreds of iterations (around 400), the

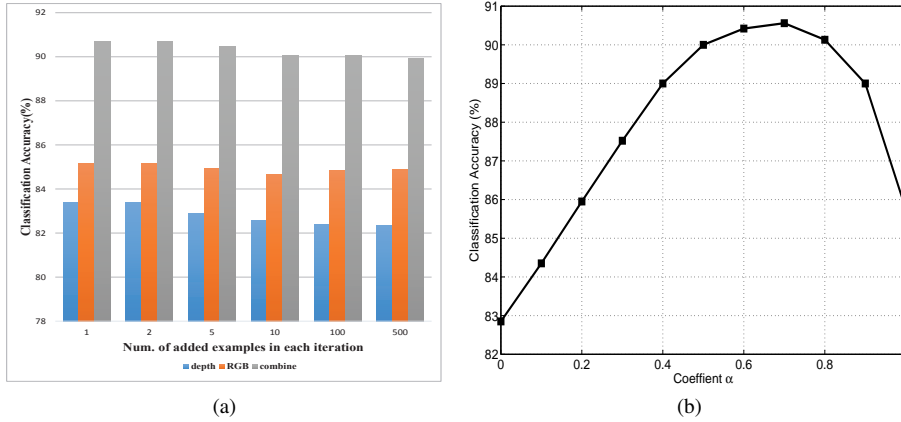


Figure 9: (a) Recognition accuracy with the added confident examples  $|n_j|$  for each class in each iteration ( $I = 500$ ,  $L = 20\%$ ,  $\alpha = 0.65$ ); (b) Recognition accuracy with the coefficient  $\alpha$  to combine the RGB view and depth view classifier ( $I = 500$ ,  $L = 20\%$ ,  $|n_j| = 2$ ).

443 recognition accuracy can rise and converge to a relatively high value, since most of the  
 444 unlabeled examples have been transferred from the unlabeled pool to the labeled pool.  
 445 This characteristic of co-training is very useful and practical as we can determine the  
 446 final iteration number from a wide range and require for high precision at the same  
 447 time.

448 (2) Influence of the labeled size of the training set. Fig. 7 also shows the labeled  
 449 size  $L$  can greatly determine the growth rate of each co-training curve and the final  
 450 recognition accuracy. When  $L$  is given a smaller size, it implies a much bigger growth  
 451 potential value along with the learning process of co-training, this is mainly because  
 452 the two initialized much weaker classifiers  $C_{RGB}$  and  $C_{depth}$  can be improved a lot  
 453 by using additional examples from the unlabeled pool. We see that a bigger size  $L$  can  
 454 keep a much higher final recognition accuracy ( $L = 1\%$ : 70.9%;  $L = 5\%$ : 83.7%;  $L =$   
 455  $10\%$ : 89.0%;  $L = 20\%$ : 90.7%). It is very reasonable since the two classifiers  $C_{RGB}$   
 456 and  $C_{depth}$  are more reliable to add examples with correct labels from the beginning to  
 457 the end, when given more labeled training examples.

458 (3) Influence of the number of added confident examples in each iteration. To keep  
 459 the balance of the size for each category in the training pool, we try to add the same  
 460 number of confident examples for each category in each iteration (i.e.,  $|n_j|$ ). Fig. 9a  
 461 reveals that the recognition results are very robust to  $|n_j|$  when it rises from 1 to 500.  
 462 Notice that the actually added examples are simultaneously constrained by the score

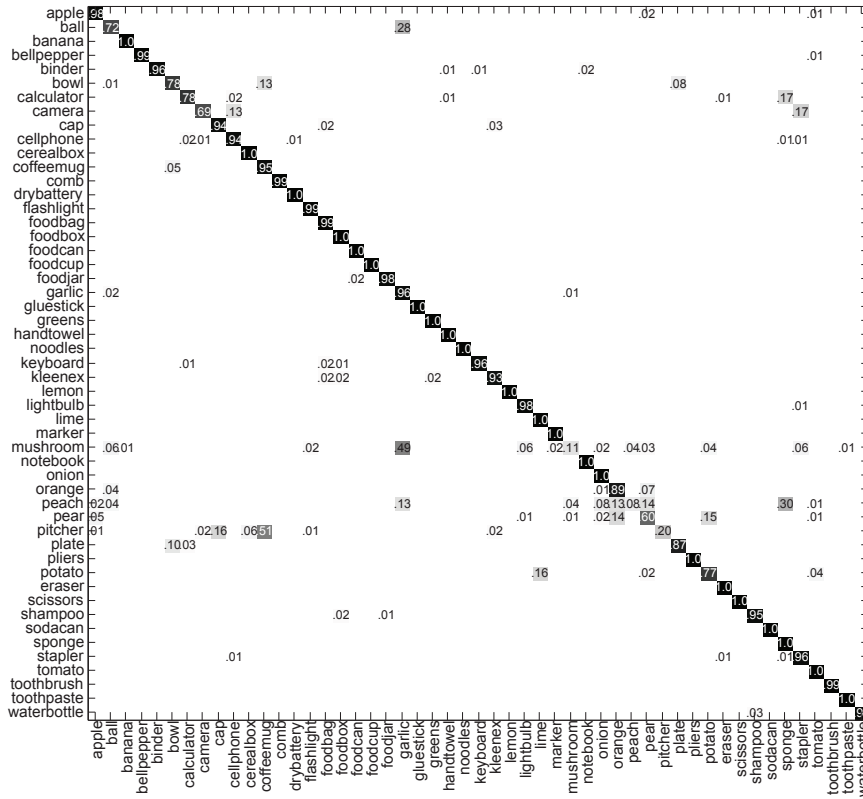


Figure 10: Confusion matrix of our semi-supervised learning method on the Washington RGB-D dataset ( $L = 20\%$ ,  $I = 500$ , CNN-SPM-RNN features). The y-axis indicates the ground true labels, and the x-axis indicates the predicted labels. Some misclassifications are: mushroom as garlic, pitcher as coffee mug

463 thresholds of  $\theta_{RGB}$  and  $\theta_{depth}$ , since we do not trust those examples with too low  
 464 scores. For the Washington RGB-D dataset, we fix  $\theta_{RGB} = \theta_{depth} = 0.1$ .

465 (4) Influence of the coefficient to combine the two view classifiers. As shown in  
 466 Fig. 9b, when change the coefficient  $\alpha$  from 0 (only using the depth classifier) to 1 (only  
 467 using the RGB classifier), the result can gradually rise to the top (when  $\alpha \in [0.5, 0.8]$ )  
 468 and then degrade. It is reasonable that object recognition can benefit a lot by regarding  
 469 both RGB view and depth view effectively.

470 We conclude that it is convenient to determine the parameter for our co-training  
 471 algorithm, since a wide range of parameters ( $I \geq 400$ ,  $L \geq 10\%$ ,  $0.5 \leq \alpha \leq$   
 472  $0.8$ ,  $|n_j| \geq 1$ ) can keep co-training successful. This characteristic is very impor-  
 473 tant and useful in practical usage. For the Washington RGB-D dataset, we select  
 474  $I = 500$ ,  $L = 20\%$ ,  $\alpha = 0.65$ ,  $|n_j| = 2$  for a balance of performance and efficiency.

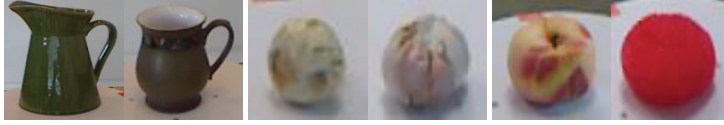


Figure 11: Examples of confused categories on the Washington RGB-D dataset. Pitcher classified as coffee mug, mushroom as garlic, and peach as sponge due to similar color or shape.

### 475 3.1.5. Error analysis

476 The confusion matrix of our semi-supervised learning method over the 51 cate-  
 477 gories is shown in Fig. 10. Most categories can be correctly classified, meaning that  
 478 our method can achieve high precision of object recognition with only a small set of  
 479 labeled data.

480 We show some examples of the often misclassified categories in Fig. 11. Mush-  
 481 rooms have almost the same appearance with garlic, pitchers look similar to coffee  
 482 mugs from some angle, and peaches have similar shape with sponges.

### 483 3.2. 2D3D Object Database

484 We also verify the effectiveness of the semi-supervised learning method on the sec-  
 485 ond public RGB-D object database, called 2D3D [5]. It consists of 156 object instances  
 486 organized into 14 categories (see examples in Fig. 12). Each instance is recorded every  
 487  $10^\circ$  around the vertical axis on a turntable, yielding 36 views per instance.

488 We also focus on category recognition. For supervised learning, we follow the  
 489 setting in [5]. We first sample 18 views for each instance and reduce the size of the  
 490 total database to 2,808 RGB-D images. Then we randomly split the database into  
 491 training and test sets, resulting in 82 instances with a total of 1476 views in the training  
 492 set, while 74 objects with 1332 views in the test set. For the semi-supervised learning,  
 493 we keep the main setting the same with the supervised. The only difference is that, we  
 494 randomly divide the training set into two parts: 20% labeled and 80% unlabeled. Note  
 495 that we also utilize additional instance labels in the process of co-training, in order to  
 496 balance the examples of each instance in the training pool  $U$ . It is very important for  
 497 co-training to bootstrap from such a small size of labeled examples.

498 Table 4 shows the results for both the supervised setting and the semi-supervised  
 499 setting. When all the training examples are labeled, CNN-SPM-RNN can achieve the  
 500 best result with 92.5% accuracy. It is worth to note that KDES ranks the second and is  
 501 superior to enhanced CKM, HMP and enhanced CNN-RNN. The main reason is prob-



Figure 12: Object examples from the 2D3D object database. Each object (RGB + depth) shown here belongs to a different category.

Methods	Labeled Size	Depth	RGB	Combine
Browatzki et al. [5]	1476	74.6	66.6	82.8
KDES [1]	1476	88.7	<b>89.1</b>	92.8
enhanced CKM	1476	87.1	82.8	88.7
HMP [3]	1476	87.6	86.3	91.0
enhanced CNN-RNN	1476	88.7	88.2	92.5
enhanced CNN-RNN+CT	328	86.0	85.3	88.2
CNN-SPM-RNN	1476	<b>89.4</b>	88.5	<b>92.9</b>
CNN-SPM-RNN+CT	328	86.0	85.4	88.4

Table 4: Comparison of results on the 2D3D object database. CT means the proposed semi-supervised learning method with co-training.

502 able that KDES takes advantage of many manually designed attributes such as object  
503 size, shape, edges, etc, which can help a lot to depict the objects than many learning  
504 based features on the relatively small scale 2D3D database. When only given 20% la-  
505 beled training set, the performance of the enhanced CNN-RNN and CNN-SPM-RNN  
506 with co-training are 88.2% and 88.4%, respectively. It is reasonable that the perfor-  
507 mance of our semi-supervised learning is lower than the supervised learning. Because  
508 co-training starts with such a few labeled examples for a multi-class recognition prob-  
509 lem, one or two added examples from the unlabeled pool  $U$  with incorrect labels can  
510 largely affect the performance of the two linear SVMs in the next round iteration.

### 511 3.3. Fusing RGB-D Object Dataset

512 The fusing RGB-D object database [41] consists of 8 classes of everyday objects  
513 (cup, bottle, doll, teddy bear, remote control, shoe, stapler, and pot, shown in Fig. 13),  
514 each with 10 objects per class. For each object, 12 images are captured by recording  
515 2 camera positions, 3 object poses and 2 illumination conditions. Thus there are 960  
516 image pairs in the database. We randomly split the database into training and test sets



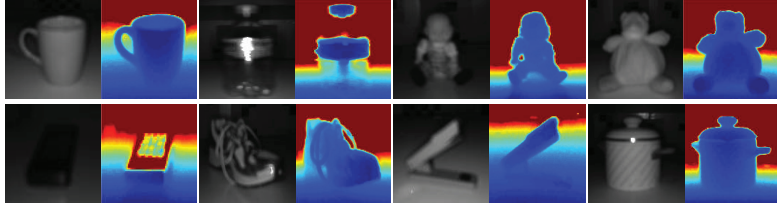


Figure 13: Object examples from the fusing RGB-D object database. Each object (RGB + depth) shown here belongs to a different category.

Methods	Labeled Size	Depth	RGB	Combine
GIFT [41]	480	80.4	77.1	84.1
3D SPMK(L=2) [42]	480	72.0	–	–
KDES [1]	480	81.0	<b>82.8</b>	<b>88.3</b>
enhanced CKM	480	83.0	77.7	87.4
HMP [3]	480	<b>84.3</b>	78.1	87.1
enhanced CNN-RNN	480	74.9	75.5	81.4
CNN-SPM-RNN	480	79.4	80.4	85.0

Table 5: Comparison of results on the fusing RGB-D dataset. Since this database has a very small scale of images, we only show the supervised results.

517 with five different objects per class in each according to [41]. Since there are a very  
 518 small scale of images, we only evaluate the performance of the supervised setting.

519 The results in Table 5 show that the well-designed kernel features of KDES can  
 520 achieve the state-of-the-art performance on the very small scale database. The main  
 521 reason is that those unsupervised feature learning methods like enhanced CKM, HMP,  
 522 CNN-RNN and CNN-SPM-RNN require a lot of training examples to achieve the dis-  
 523 criminating abilities. And for depth modality, such effects by the small scale of training  
 524 set are even more remarkable for enhanced CNN-RNN and CNN-SPM-RNN.

#### 525 4. Conclusion

526 This paper proposes a semi-supervised learning framework based on co-training  
 527 for RGB-D object recognition, which can exploit the two distinct views (RGB and  
 528 depth) to boost the performance by learning from the unlabeled data. Through the  
 529 analysis of the state-of-the-art features along with an unbiased evaluation, we find out  
 530 that the proposed CNN-SPM-RNN features are very powerful to represent the RGB-D  
 531 objects. The experiments demonstrate the effectiveness of our method, especially for  
 532 large scale RGB-D datasets, since both the CNN-SPM-RNN features and the semi-  
 533 supervised learning model can benefit from more available data. Furthermore, our

534 method is lowly sensitive to the selection of the parameter values such as the labeled  
535 training size, the iteration number, etc. We believe our method can be a useful tool  
536 for many vision applications, e.g, RGB-D dataset annotation and robot navigation, by  
537 solving the expensive and difficult task of manually labeling massive data.

538 In addition, this paper also provides a meaningful guideline how to better repre-  
539 sent RGB-D objects. For large scale RGB-D object datasets, e.g., the Washington  
540 RGB-D dataset, those unsupervised feature learning methods such as enhanced CK-  
541 M, HMP, enhanced CNN-RNN and CNN-SPM-RNN can achieve higher recognition  
542 performance. While for small scale RGB-D object datasets, e.g., the fusing RGB-D  
543 dataset, the well-designed kernel descriptors on top of various attributes such as object  
544 shape, size, edges, etc. are the best choice to depict objects.

545 In future work, we will try to use on-line learning algorithms to improve the effi-  
546 ciency of the semi-supervised learning framework.

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